

$$(a) \quad 2 = \lim_{x \rightarrow 3} \frac{f(x)}{2x} + \lim_{x \rightarrow 3} (1) \quad \Rightarrow \quad 2 = \lim_{x \rightarrow 3} \frac{f(x)}{2x} + 1$$

$$\Rightarrow 1 = \lim_{x \rightarrow 3} \frac{f(x)}{2x}$$

$$\lim_{x \rightarrow 3} 2x = 6 \neq 0$$

$$1 = \frac{\lim_{x \rightarrow 3} f(x)}{\lim_{x \rightarrow 3} 2x}$$

$$\Rightarrow 1 = \frac{\lim_{x \rightarrow 3} f(x)}{6} \quad \Rightarrow \quad \boxed{6} = \lim_{x \rightarrow 3} f(x)$$

$$\begin{aligned} (b) \quad \lim_{x \rightarrow 0} \frac{\tan(4x)}{\sin(6x)} &= \lim_{x \rightarrow 0} \frac{\sin(4x)}{\cos(4x)} \cdot \frac{1}{\sin(6x)} \\ &= \lim_{x \rightarrow 0} \frac{4}{6} \frac{\sin(4x)}{4x} \cdot \frac{6x}{\sin(6x)} \cdot \frac{1}{\cos(4x)} \\ &= \frac{4}{6} \left(\lim_{x \rightarrow 0} \frac{\sin(4x)}{4x} \right) \left(\lim_{x \rightarrow 0} \frac{6x}{\sin(6x)} \right) \left(\lim_{x \rightarrow 0} \frac{1}{\cos(4x)} \right) \\ &= \frac{4}{6} (1)(1)(1) = \boxed{\frac{4}{6}} \end{aligned}$$

$$\begin{aligned} (c) \quad \lim_{x \rightarrow \infty} \frac{-2x^3 + 2x + 3}{3x^3 + 3x^2 - 3} &= \lim_{x \rightarrow \infty} \frac{-2x^3 - 2x + 3}{3x^3 + 3x^2 - 3} \cdot \frac{\left(\frac{1}{x^3}\right)}{\left(\frac{1}{x^3}\right)} \\ &= \lim_{x \rightarrow \infty} \frac{-2 - \frac{2}{x^2} + \frac{3}{x^3}}{3 + \frac{3}{x} - \frac{3}{x^3}} \\ &= \frac{\lim_{x \rightarrow \infty} \left(-2 - \frac{2}{x^2} + \frac{3}{x^3}\right)}{\lim_{x \rightarrow \infty} \left(3 + \frac{3}{x} - \frac{3}{x^3}\right)} = \boxed{\frac{-2}{3}} \end{aligned}$$